

You have 1 hour to complete all questions and show your working where applicable.
There are 60 marks available. You may use a calculator.

1. Simplify the following expressions.

(a) $\frac{a^2 \times a^5}{a^3}$

..... a^4 (1)

(b) $\frac{(3x^2)^3}{x^{-4}}$

$= \frac{27x^6}{x^{-4}}$

..... $27x^{10}$ (1)

(c) $\frac{2y^{1/2}}{(8y^{-3})^{2/3}}$

$= \frac{2y^{1/2}}{4y^{-2}}$

..... $\frac{1}{2}y^{5/2}$ (1)

2. Solve the following equations.

(a) $3n^2 \times 4n^3 = 384$

$12n^5 = 384$

$n^5 = 32$

$n = 2$

$n = \dots 2$ (1)

(b) $3 \times \sqrt{27} = 3^x$

$3 \times 3^{3/2}$ (1)

$= 3^{5/2}$

$x = \dots \frac{5}{2}$ (1)

(c) $a^{-3/4} = \frac{1}{27}$

$a^{3/4} = 27$

$a^{1/4} = 3$ (1)

$a = \dots 81$ (2)

3. Simplify the following surds. You must show your working.

(a) $\sqrt{72}$

..... $6\sqrt{2}$ (1)

(b) $\sqrt{32} \times \sqrt{45}$

$4\sqrt{2} \times 3\sqrt{5}$

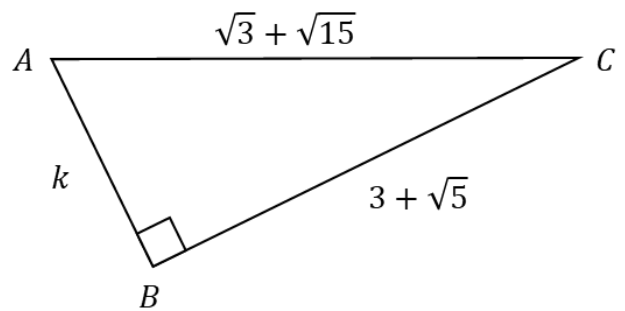
..... $12\sqrt{10}$ (1)

(c) $(2 + \sqrt{5})(1 - \sqrt{5})$

$$\begin{array}{r|rr} & 2 & +\sqrt{5} \\ 1 & 2 & +\sqrt{5} \\ -\sqrt{5} & -2\sqrt{5} & -5 \end{array}$$
 (1)

..... $-3 - \sqrt{5}$ (2)

4. All measurements on the triangle are in centimetres.
 ABC is a right-angled triangle. k is a positive integer.
 Find the value of k .
 You must show your working.



$$\begin{aligned} k^2 &= (\sqrt{3} + \sqrt{15})^2 - (3 + \sqrt{5})^2 \quad (1) \\ &= 18 + 6\sqrt{5} - (14 + 6\sqrt{5}) \\ &= 4 \quad (1) \\ k &= 2 \end{aligned}$$

$$k = \dots\dots\dots 2 \dots\dots\dots (3)$$

5. Rationalise the denominator of these surds. You must show your working.

(a) $\frac{1}{\sqrt{5}}$

$$\frac{1}{\sqrt{5}} \times \frac{\sqrt{5}}{\sqrt{5}}$$

$$\frac{\sqrt{5}}{5} \quad (1)$$

.....

(b) $\frac{6}{2\sqrt{3}}$

$$\begin{aligned} \frac{6}{2\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}} \\ = \frac{6\sqrt{3}}{6} \quad (1) \end{aligned}$$

$$\sqrt{3} \quad (1)$$

.....

(c) $\frac{5+2\sqrt{3}}{2+\sqrt{3}}$

$$\begin{aligned} \frac{(5+2\sqrt{3})(2-\sqrt{3})}{(2+\sqrt{3})(2-\sqrt{3})} \quad (1) \\ = \frac{4-\sqrt{3}}{1} \quad (1) \end{aligned}$$

$$4 - \sqrt{3} \quad (1)$$

..... (3)

6. Expand and simplify these expressions.

(a) $4x(xy + 3)$

(b) $(x + 3)(2x - 4)$

(c) $(x - 3)^2(x + 2)$

$$\begin{array}{r|rr} & x & +3 \\ 2x & 2x^2 & +6x \\ -4 & -4x & -12 \end{array} \quad (1)$$

$$\begin{array}{r|rr} & x & -3 \\ x & x^2 & -3x \\ -3 & -3x & +9 \end{array} \quad (1)$$

$$\begin{array}{r|rrr} & x^2 & -6x & +9 \\ x & x^3 & -6x^2 & +9x \\ +2 & +2x^2 & -12x & +18 \end{array} \quad (1)$$

$$4x^2y + 12x \quad (1)$$

.....

$$2x^2 + 2x - 12 \quad (1)$$

.....

$$x^3 - 4x^2 - 3x + 18 \quad (1)$$

..... (3)

7. Fully factorise these expressions.

(a) $6a^2b - 9ab^3$

① Any correct factor

$3ab(2a+3b^2)$ (2)

(b) $x^2 - x - 42$

① $(x+7)(x-6)$

$(x-7)(x+6)$ (2)

(c) $6x^2 + 7x - 3$

$$\begin{array}{r|rr} & 2x & +3 \\ 3x & 6x^2 & +9x \\ -1 & -2x & -3 \end{array}$$
 ①

$(3x-1)(2x+3)$ (2)

8. Solve the following equations.

(a) $4a + 6 = 8$

$4a = 2$

$a = \frac{1}{2}$ ①

(b) $x^2 - 7x + 12 = 0$

$(x-3)(x-4) = 0$ ①

$x = 3 \text{ or } 4$ ①

(c) $2n^2 + 3n = 11 - n$

$2n^2 + 4n - 11 = 0$ ①

$$n = \frac{-4 \pm \sqrt{4^2 - 2 \times 2 \times -11}}{2 \times 2}$$
 ①

$n = 1.55 \text{ or } -3.55$ ①

9. (a) Write $x^2 + 10x + 2$ in the form $(x + a)^2 + b$ where a and b are integers.

$(x+5)^2 + 2 - 5^2$ ①

$(x+5)^2 - 23$ (2)

(b) Hence, or otherwise, write down the coordinates of the turning point of the graph of $y = x^2 + 10x + 2$

$(-5, -23)$ ① (1)

10. Given that $f(x) = 2x^2 - 10$,

(a) find $f(-2)$

$2(-2)^2 - 10$

-2 ① (1)

(b) Solve $f(x) = 8$

$2x^2 - 10 = 8$ ①

$2x^2 = 18$ ①

$x^2 = 9$

$x = 3 \text{ or } -3$ ① (3)

11. Solve these pairs of simultaneous equations. You must show your working.

(a) $3x - y = -4$ $\times 3$
 $2x - 3y = 9$

$$\begin{array}{r} 9x - 3y = -12 \\ -2x - 3y = 9 \end{array} \quad \left. \vphantom{\begin{array}{r} 9x - 3y = -12 \\ -2x - 3y = 9 \end{array}} \right\} \textcircled{1}$$

$$7x = -21$$

$$x = -3 \quad \textcircled{1}$$

$$3x - y = -4$$

$$-9 - y = -4$$

$$y = -5 \quad \textcircled{1}$$

(b) $x^2 + y^2 = 17$
 $y = x - 3$

$$x^2 + (x - 3)^2 = 17 \quad (1)$$

$$2x^2 - 6x - 8 = 0$$

$$x^2 - 3x - 4 = 0 \quad (1)$$

$$(x - 4)(x + 1) = 0 \quad (1)$$

$$x = 4 \quad \text{or} \quad -1 \quad (1)$$

\downarrow
 $y = 4 - 3 = 1$

\downarrow
 $y = -1 - 3 = -4 \quad (1)$

$$\begin{aligned} x &= \dots -3 \dots \\ y &= \dots -5 \dots \end{aligned} \quad (3)$$

$$\begin{aligned} x &= \dots 4 \text{ or } -1 \dots \\ y &= \dots 1 \text{ or } -4 \dots \end{aligned} \quad (5)$$


12. Solve these inequalities. You must show all your working.

(a) $3x - 7 \geq 2$
 $3x \geq 9$
 ①

(b) $-7 < 2x + 3 < 1$
 $-10 < 2x < -2$
 $-5 < x < -1$

(c) $x^2 - 7x + 6 < 0$

$(x-1)(x-6) < 0$



$$x \geq 3 \quad (1)$$

(2) $-5 < x < -1$ (2)

$$\textcircled{1} \quad 1 < x < 6 \quad (2)$$